

# Maths workshop

Tuesday 3<sup>rd</sup> December



altogether

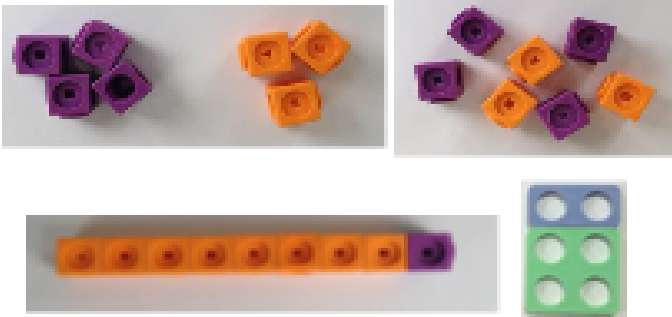

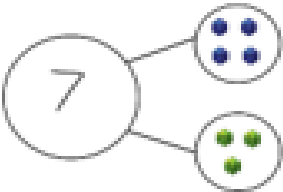
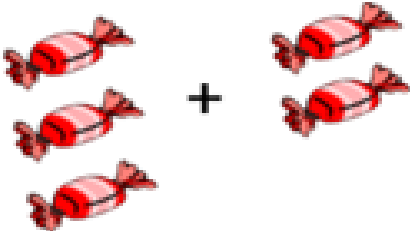
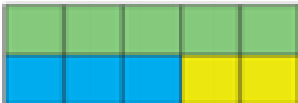
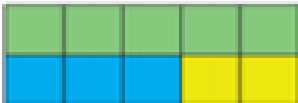

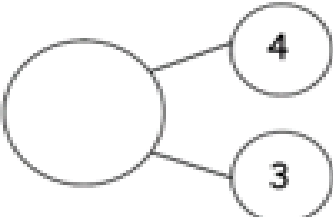
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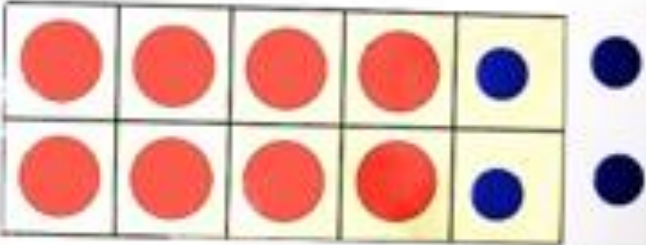



add

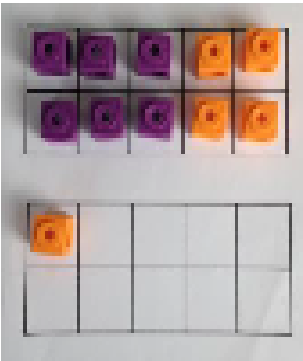

**Addition**

plus

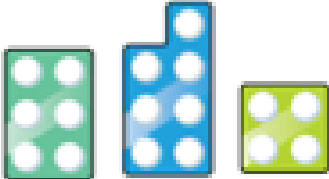


sum

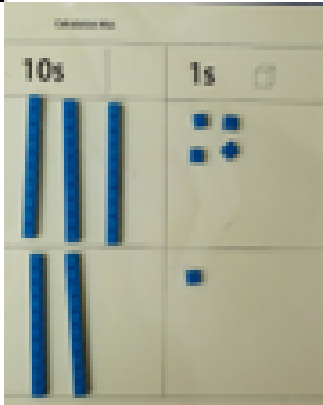

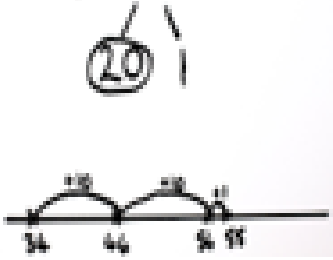


Objective and Strategies	Concrete	Pictorial	Abstract
<p>Combining two parts to make a whole: part-whole model</p>	<p>Use a variety of concrete items, eg. cubes, toys, Cuisenaire rods and Numicon, to add two numbers together, as a group. Placing cubes in a bar formation builds understanding of the bar model.</p>   <p>Place concrete equipment on a part-whole model.</p> <p>One part is 4, one part is 3, the whole is 7.</p> 	<p>Use given pictures to add two numbers together, as a group. Pictures can be shown in a bar formation. Children can then progress to drawing their own pictures, or dots, to represent the numbers.</p>   <p>Link work with cubes, to the bar model, by initially shading individual squares, to represent the numbers.</p>  	<p>Use numerical recording, alongside concrete and pictorial representations, to help children progress towards an abstract understanding of numbers. Build on the use of a part-whole model.</p>  <p> <math>4 + 3 = 7</math>  <math>3 + 4 = 7</math>  <math>7 = 3 + 4</math>  <math>7 = 4 + 3</math> </p> <p>Ensure children explore commutativity and regularly encounter the = symbol at the beginning of calculations, as well as calculations involving 0.</p>

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Starting at the bigger number and counting on</p>	<p>Children represent the larger number, using concrete equipment, and then count on in 1s, while adding the correct number of beads, counters etc.</p> <p><math>8 + 4 = 12</math></p>  <p><math>12 + 5 = 17</math></p> 	<p>Children progress to counting on using a number track, then a number line. Placing cubes on a number track, can help to reinforce children's understanding of the number sequence.</p>   <p><math>12 + 5 = 17</math></p> <p>Circle the larger number. Count on in ones. How many have you got altogether?</p>	<p>Children can begin to calculate mentally, by placing the larger number in their head and counting on in 1s, using their fingers to keep track of the count.</p> <p><math>5 + 12 = 17</math></p> <p>Put the larger number in your head. Count on in ones. How many have you got altogether?</p>

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Regrouping to make 10.</p>	<p>Children can begin to calculate more efficiently, by partitioning the number to be added. They make a whole group of 10 first, then add the remainder.</p> <p><math>6 + 5 = 11</math></p>  <p>Start with the larger number. How many more do you need to make 10? How many have you got left to add?</p>	<p>Children can show their understanding of regrouping using a number line.</p> 	<p>Children regroup mentally, in order to add efficiently.</p> <p><math>7 + 4 = 11</math></p> <p>Start with the larger number. How many more do you need to make 10? How many have you got left to add?</p>

**\* To do this they have to be secure with their number bonds to 10.**

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Adding three single digits</p>	<p>Children can calculate efficiently, by looking for pairs of numbers that total 10, then adding the third number.</p> $4 + 7 + 6 = 10 + 7 = 17$   		$\textcircled{4} + 7 + \textcircled{6} = 10 + 7 = 17$ <p>Add the two numbers that make 10. Then add the remaining number.</p>

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Adding 2-digit numbers mentally, using equipment or pictorial support</p>	<p>Represent the calculation on a calculation mat, using Base 10. Children total the equipment, starting their count with the 10s and then counting on to the 1s.</p> 	<p>Children can then draw Base 10 and total, as with concrete equipment.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> <math>34 + 21 = 55</math>   </div> <div style="text-align: center;"> <math>34 + 21 = 55</math>   </div> </div> <p>Some children find it helpful to draw a number line, or bar, to visualise their calculation.</p> 	<p>Children partition the numbers and recombine, to support them in calculating mentally.</p> <div style="text-align: center;"> <math>34 + 21 = 50 + 5 = 55</math>   </div>

subtract

difference

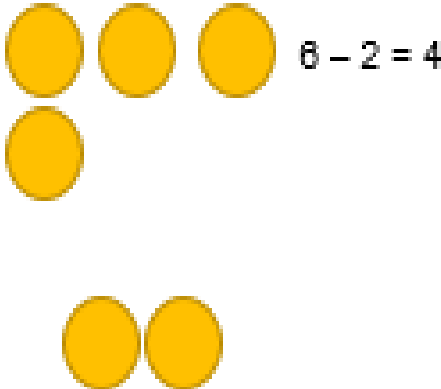
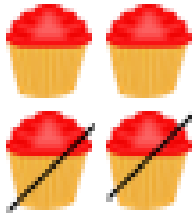
minus

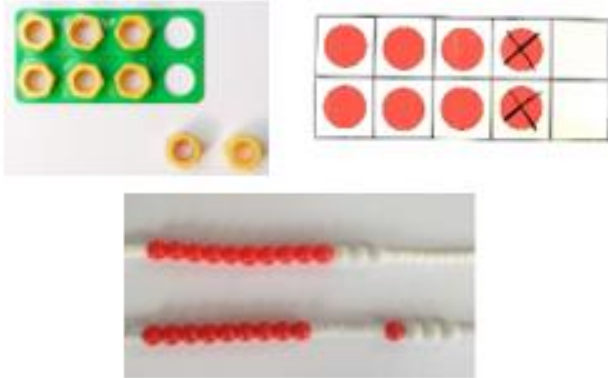
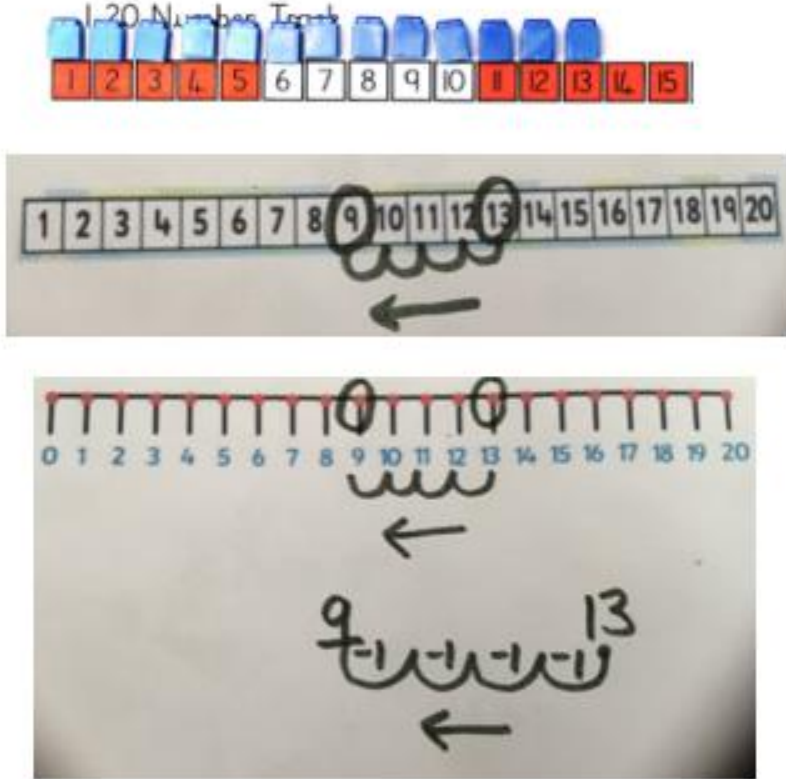
**Subtraction**

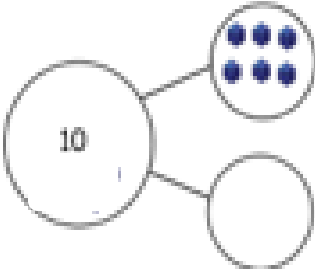

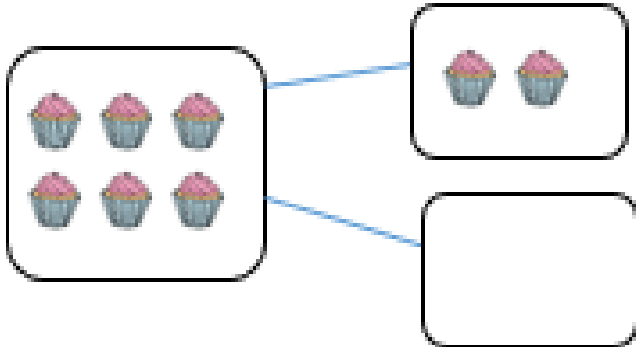
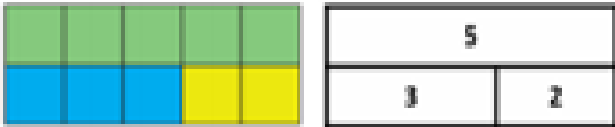
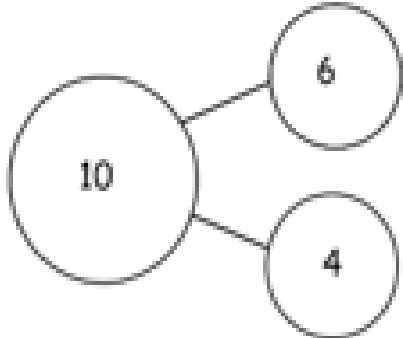
less


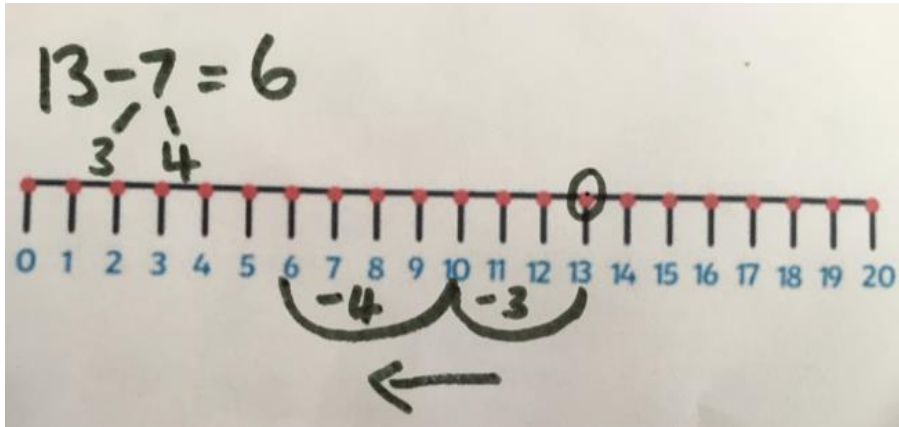
take away

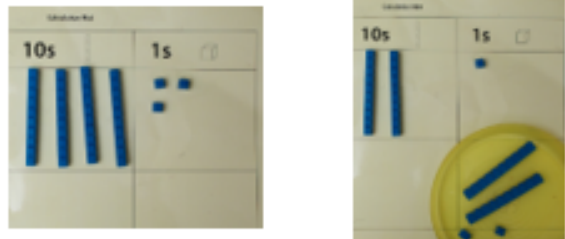
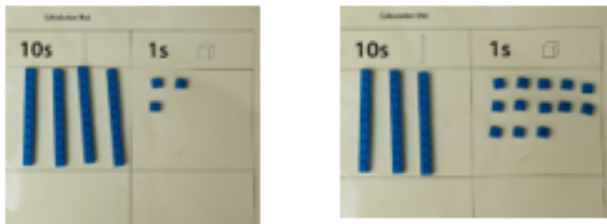

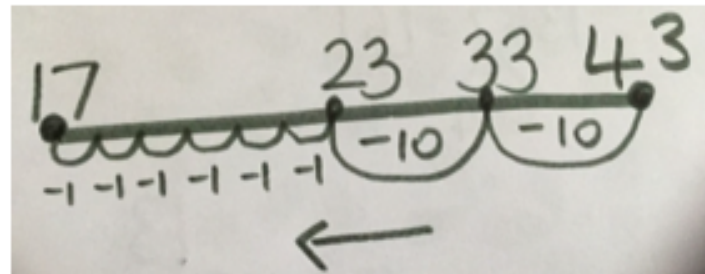



Objective and Strategies	Concrete	Pictorial	Abstract
<p>Taking away ones</p>	<p>Use a variety of concrete items eg. toys, counters, cubes, to model taking a number away from a group.</p>  $8 - 2 = 6$	<p>Cross out drawn objects to show what has been taken away.</p>  $8 - 2 = 6$	<p>Use numerical recording, alongside concrete and pictorial representations, to help children progress towards an abstract understanding of numbers.</p> $8 - 2 = 6$

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Counting back</p>	<p>Represent the larger number using concrete equipment. Count back in ones, as you remove the correct number of beads / cubes.</p> 	<p>Placing cubes on a number line makes links between different representations. Children can count back using a number track, then number line.</p>  <p>Circle the larger number. Count back in 1s. How many have you got left?</p>	<p>Children can begin to calculate mentally, by placing the larger number in their head and counting back in 1s, using their fingers to keep track of the count.</p> <p><math>13 - 4 = 9</math></p> <p>Put the larger number in your head. Count back in ones. How many have you got left?</p>

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Relate subtraction to addition</p>	<p>Use part whole models and cuisenaire rods to help children understand the inverse relationship between addition and subtraction.</p>  <p>10 is the whole. 6 is one of the parts. What is the other part?</p> <p>9-2 </p>	<p>Use a pictorial representation of objects to show the part whole model.</p>  <p>Use the bar model to help children find related addition and subtraction calculations.</p> 	<p>Children can progress to recording numbers within the part whole model.</p>  <div> <div> <math>6 + 4 = 10</math>  <math>4 + 6 = 10</math>  <math>10 - 4 = 6</math>  <math>10 - 6 = 4</math> </div> <div> <math>10 = 6 + 4</math>  <math>10 = 4 + 6</math>  <math>6 = 10 - 4</math>  <math>4 = 10 - 6</math> </div> </div>

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Regrouping to make 10</p>	<p>As with addition, children can begin to calculate more efficiently, by partitioning the number to be subtracted. They subtract part of the number, to leave a multiple of 10, and then subtract the remainder</p> <p><math>14 - 5 = 9</math></p> 	<p>Children can show their understanding of regrouping, using a number line.</p> 	<p>Children regroup mentally, in order to subtract efficiently.</p> <p><math>13 - 7 = 6</math></p> <p>How many do you need to subtract to leave 10? How many have you got left to subtract?</p>

Objective and Strategies	Concrete	Pictorial	Abstract
<p><b>Subtracting 2-digit numbers using equipment or pictorial support</b></p>	<p>Represent the calculation on a calculation mat, using Base 10. Children remove the number to be subtracted. They count the equipment that remains</p> $43 - 22 = 21$  <p>Where regrouping is required, children can exchange one 10 for ten 1s, before subtracting.</p> $43 - 26 =$  <p>They can now subtract 26.</p>	<p>Children can then draw Base 10 and cross out the number they are subtracting. They count the remaining number, to find out how many are left.</p> $55 - 21 = 34$  <p>When regrouping is required, children can cross out one ten, and draw ten 1s in its place, before subtracting.</p> <p>Children can also draw a number line, to support mental calculation.</p> 	<p>Children partition the number to be subtracted, to support them in calculating mentally.</p> $43 - 26 = 23 - 6 = 17$ 

repeated addition

multiply

groups of

**Multiplication**

times

array

double

Objective and Strategies

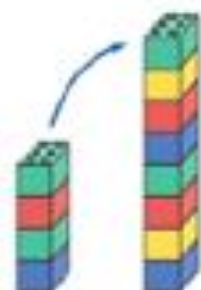
Concrete

Pictorial

Abstract

Doubling

Use practical activities to show how to double a number.



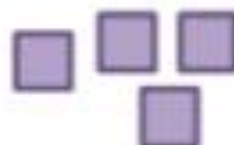
double 4 is 8

$$2 \times 4 = 8$$

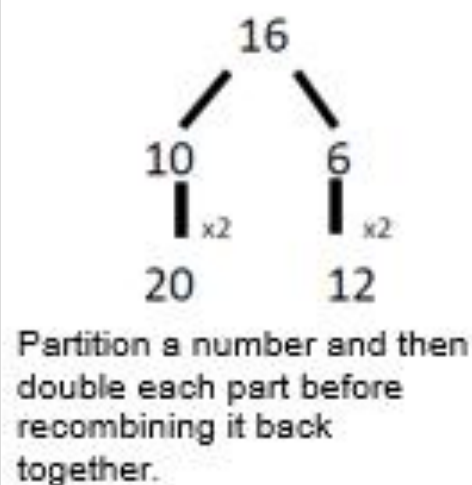


Draw pictures to show how to double a number.

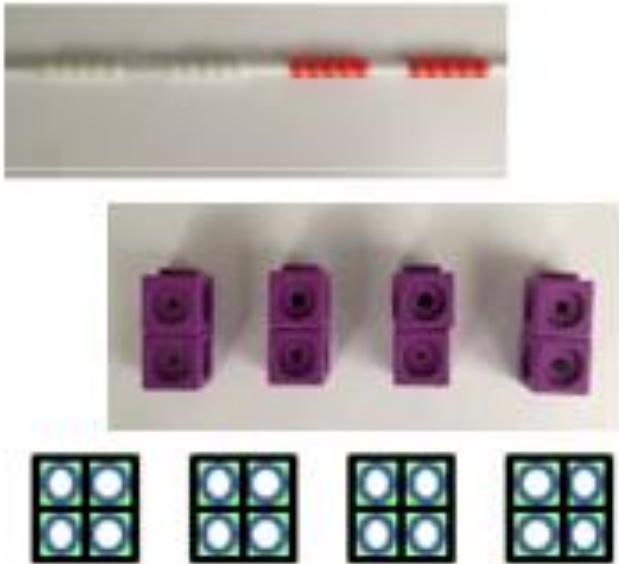

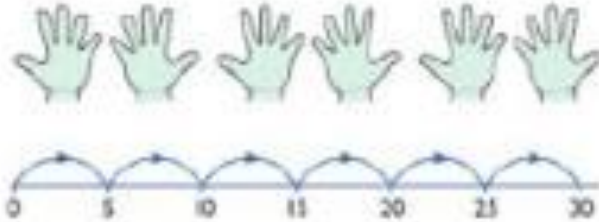

Double 4 is 8



Double  is





Objective and Strategies	Concrete	Pictorial	Abstract								
<p>Counting in multiples</p>	 <p>Count in multiples supported by concrete objects in equal groups.</p>  <p>Use Cuisenaire rods to support use of model</p>	 <p>Use a number line or pictures to continue support in counting in multiples.</p>  <p>Bar model shows relationship between whole/ parts and makes links to division.</p> <table border="1" data-bbox="1490 906 1989 1029"> <tr> <td colspan="4">12</td></tr> <tr> <td>3</td><td>3</td><td>3</td><td>3</td></tr> </table>	12				3	3	3	3	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>
12											
3	3	3	3								



Objective and Strategies	Concrete	Pictorial	Abstract
<p>Repeated addition – linking to multiplication</p>	<div data-bbox="453 261 759 401"></div> <div data-bbox="792 234 1021 391"> <math>5 + 5 + 5 = 15</math>  3 groups of 5 equals 15  <math>3 \times 5 = 15</math> </div> <div data-bbox="412 419 787 634"></div> <div data-bbox="461 572 715 625"> <math>3 + 3 + 3</math> </div> <div data-bbox="843 415 1065 634"></div> <div data-bbox="422 662 705 791"> <math>3 + 3 + 3 = 9</math>  <math>3 \times 3 = 9</math>  3 groups of 3 = 9 </div> <div data-bbox="422 876 1047 955"> Use Cuisenaire rods to show repeated addition </div> <div data-bbox="422 1076 843 1230"></div>	<p>There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?</p> <div data-bbox="1123 319 1276 419"></div> <div data-bbox="1505 319 1658 419"></div> <div data-bbox="1875 305 2028 419"></div> <div data-bbox="1429 434 1709 469"> 2 add 2 add 2 equals 6 </div> <div data-bbox="1365 476 1773 519"> 3 groups of 2 = <math>3 \times 2 = 6</math> </div> <div data-bbox="1136 562 1735 676"></div> <div data-bbox="1798 605 2015 641"> <math>5 + 5 + 5 = 15</math> </div> <div data-bbox="1378 691 1811 733"> 3 groups of 5 = <math>3 \times 5 = 15</math> </div> <div data-bbox="1238 748 1658 862"></div>	<p>Write addition sentences to describe objects and pictures.</p> <div data-bbox="2066 462 2499 576"></div> <div data-bbox="2181 576 2410 605"> <math>2 + 2 + 2 + 2 + 2 = 10</math> </div> <div data-bbox="2053 705 2486 748"> 5 groups of 2 = <math>5 \times 2 = 10</math> </div>

# Objective and Strategies

## Concrete

## Pictorial

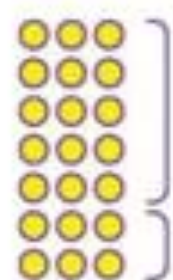
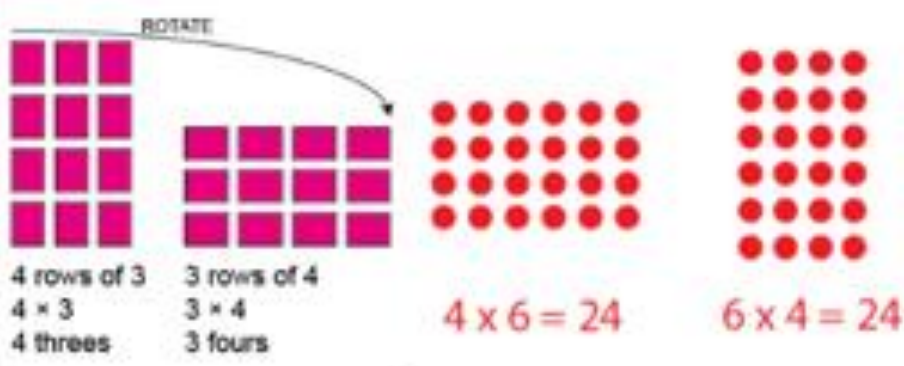
## Abstract

### Arrays- showing commutative multiplication

Create arrays using counters/ cubes to show multiplication sentences.



Draw arrays in different rotations to find commutative multiplication sentences.



Children use their knowledge of known multiplication tables

This  $3 \times 7$  array can also be seen as  $3 \times 5$  and  $3 \times 2$

$$7 \times 3 = 21$$

$$3 \times 7 = 21$$

Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

$$3 + 3 + 3 + 3 + 3 = 15$$

$$5 \times 3 = 15$$

$$3 \times 5 = 15$$

Commutative Property	Repeated Addition
$3 \times 5 = 16$	$5 + 5 + 5 = 15$
Groups of: 	An Array: 
3 groups of 5	

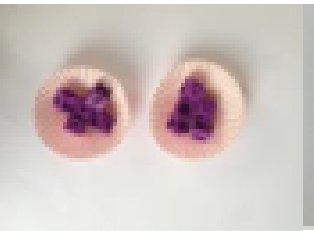
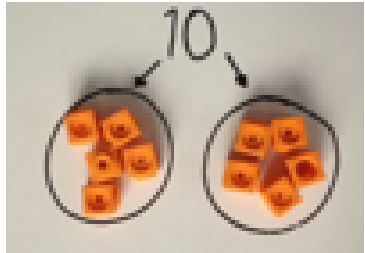
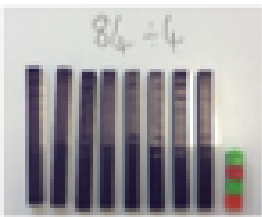

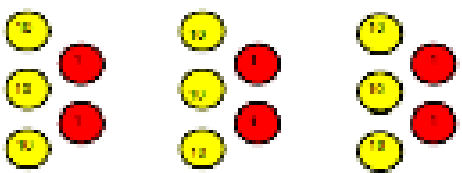

divided by

shared by

# Division

half

equal groups  
of

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Sharing objects into groups</p>	<div data-bbox="415 178 726 406">  </div> <div data-bbox="759 199 1039 364"> <p>I have 10 cubes, can you share them equally in 2 groups?</p> </div> <div data-bbox="415 421 777 671">  </div> <div data-bbox="606 678 866 892">  </div> <div data-bbox="509 899 963 1028">  </div> <div data-bbox="580 1042 845 1099"> <p><math>96 \div 3 = 32</math></p> </div> <div data-bbox="504 1149 963 1320">  </div>	<p>Children use pictures or shapes to share quantities.</p> <div data-bbox="1100 242 1872 535">  </div> <div data-bbox="1324 564 1702 656"> <p><math>8 \div 2 = 4</math></p> </div>	<p>Share 9 buns between three people.</p> <p><math>9 \div 3 = 3</math></p>

# Objective and Strategies

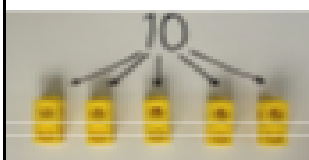
## Concrete

## Pictorial

## Abstract

### Division as grouping

Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.

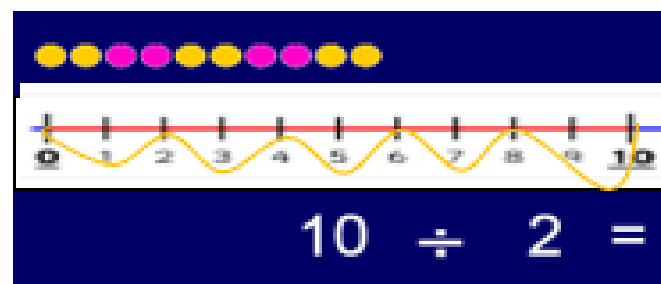


12



$$20 \div 5 = 4$$

Use a number line to show jumps in groups. The number of jumps equals the number of groups.



Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.


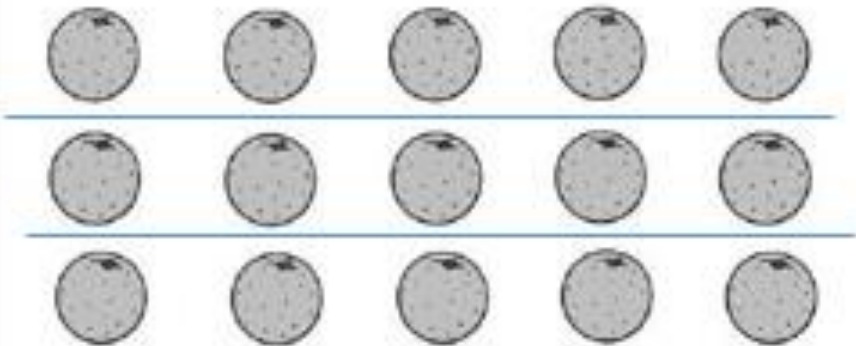
$$20 \div 4 = 5$$

20 divided into groups of 4 equals 5



$$28 \div 7 = 4$$

Divide 28 into 7 groups. How many are in each group?

Objective and Strategies	Concrete	Pictorial	Abstract
<p>Division within arrays</p>	<div data-bbox="417 354 817 611">  </div> <p data-bbox="843 361 1059 646">Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p data-bbox="422 732 868 811">Eg <math>15 \div 3 = 5</math>    <math>5 \times 3 = 15</math>  <math>15 \div 5 = 3</math>    <math>3 \times 5 = 15</math></p>	<div data-bbox="1105 354 1956 696">  </div> <p data-bbox="1116 732 2033 811">Draw an array and use lines to split the array into groups to make multiplication and division sentences.</p>	<p data-bbox="2074 318 2512 475">Find the inverse of multiplication and division sentences by creating four linking number sentences.</p> <p data-bbox="2074 525 2244 689"> <math>7 \times 4 = 28</math>  <math>4 \times 7 = 28</math>  <math>28 \div 7 = 4</math>  <math>28 \div 4 = 7</math> </p>

## Working at the expected standard

- add and subtract any 2 two-digit numbers using an efficient strategy, explaining their method verbally, in pictures or using apparatus (e.g.  $48 + 35$ ;  $72 - 17$ )
- recall all number bonds to and within 10 and use these to reason with and calculate bonds to and within 20, recognising other associated additive relationships (e.g. If  $7 + 3 = 10$ , then  $17 + 3 = 20$ ; if  $7 - 3 = 4$ , then  $17 - 3 = 14$ ; leading to if  $14 + 3 = 17$ , then  $3 + 14 = 17$ ,  $17 - 14 = 3$  and  $17 - 3 = 14$ )
- recall multiplication and division facts for 2, 5 and 10 and use them to solve simple problems, demonstrating an understanding of commutativity as necessary

## Working at greater depth

- use reasoning about numbers and relationships to solve more complex problems and explain their thinking (e.g.  $29 + 17 = 15 + 4 + \square$ ; 'together Jack and Sam have £14. Jack has £2 more than Sam. How much money does Sam have?' etc.)
- solve unfamiliar word problems that involve more than one step (e.g. 'which has the most biscuits, 4 packets of biscuits with 5 in each packet or 3 packets of biscuits with 10 in each packet?')

11

$68 + 20 = \boxed{\phantom{00}}$



11

$68 + 20 = \boxed{88}$



68  
+10 +10  
88

12

$7 + 84 = \boxed{\phantom{00}}$



12

$7 + 84 = \boxed{91}$



84  
+1 +1 +1 +1 +1 +1 +1  
91



24 Sam plays a maths game.

Each  is equal to 2 points.


 +  +  = 10 points




How many points is **one**  equal to?


points

1 mark

24 Sam plays a maths game.

Each  is equal to 2 points.

 + <sup>2</sup> + <sup>2</sup> = 10 points

How many points is **one**  equal to?

6

points

1 mark

$2+2=4$   
 $10-4=6$

29 There are **100g** of chocolate chips in the bag.

Sita uses **25g**.

Ben uses **35g**.



How many grams of chocolate chips are **left** in the bag?

Show  
your  
working

g

2 marks

29 There are **100g** of chocolate chips in the bag.

Sita uses **25g**.

Ben uses **35g**.



How many grams of chocolate chips are **left** in the bag?

Show  
your  
working

$111\frac{1}{4} + 111\frac{1}{4} = 60$

$100 - 10 - 10 - 10 - 10 - 10 = 40$

40

g

2 marks